



**Motion and Forces in a Gravitational Field: World records and fun fairs – Comprehension**

set	number	solution												
Comp1	1	Short arms – you raise the weight through a shorter distance so do less work against gravity												
	2a	Power = work done / time Estimate length of arms = 1 m. Work done = force × distance moved = $138 \times 10^3 \text{ kg} \times 9.81 \text{ N kg}^{-1} \times 1 \text{ m} = 1.35 \times 10^6 \text{ J}$ Power = work done / time = $1.35 \times 10^6 \text{ J} / 3600 \text{ s} = 375 \text{ W}$												
	2b	$375 \text{ W} / 0.746 \text{ kW} = 0.50$ Bench presser has a horsepower of 0.5.												
	3	A reasonable estimate following the trend would be larger than 250 km /h. This is probably an unreliable prediction. Some reasons would be : do people actually want to travel that fast, the improvements have been only small indicating that technology isn't changing just being slightly improved so unlikely to keep on increasing, safety concerns.  <div style="text-align: center;"> <p>trends for rollercoasters</p> <table border="1"> <caption>Data for trends for rollercoasters</caption> <thead> <tr> <th>Year of completion</th> <th>Max speed (km/h)</th> </tr> </thead> <tbody> <tr> <td>1996</td> <td>130</td> </tr> <tr> <td>2000</td> <td>145</td> </tr> <tr> <td>2001</td> <td>170</td> </tr> <tr> <td>2003</td> <td>190</td> </tr> <tr> <td>2005</td> <td>205</td> </tr> </tbody> </table> </div>	Year of completion	Max speed (km/h)	1996	130	2000	145	2001	170	2003	190	2005	205
Year of completion	Max speed (km/h)													
1996	130													
2000	145													
2001	170													
2003	190													
2005	205													
	3a	Equating g.p.e. and k.e. leads to $v = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 127} = 49.9 \text{ m s}^{-1}$												
	3b	Answer to 3a is less than $200 \text{ km h}^{-1}$ (equivalent to $55.5 \text{ m s}^{-1}$ ). This is probably because the rollercoaster doesn't just 'drop' it will also have a motor to accelerate it downwards in addition to the acceleration provided by gravity.												
	5a	Resolving horizontally $t = 128/u \cos 45^\circ$ Substitute into $s = ut + \frac{1}{2}at^2$ (vertically) $-1 = \frac{u \sin 45^\circ \times 128}{u \cos 45^\circ} + \frac{1}{2} \times -9.8 \times \frac{128^2}{u^2 \cos^2 45^\circ}$ $-129 u^2 \cos^2 45^\circ = -80300$ $u = 35.3 \text{ m s}^{-1}$												
	5b	See diagram on page 21 of Exploring Physics												
	5c	Vertically when $s = s_{\text{max}}$ $v = 0$ $s = \frac{u^2}{2a} = \frac{(35.3 \times \sin 45^\circ)^2}{2 \times 9.8}$ $s = 31.8 \text{ m s}^{-1}$												
	5d	Use the same method as 5a, $-54.65 u^2 = -80300$ $u = 38.3 \text{ m s}^{-1}$												
	6a	$400 \text{ km h}^{-1} = 111 \text{ m s}^{-1}$ $a = \frac{v^2}{r} = \frac{111^2}{450} = 27.4 \text{ m s}^{-2}$ $27.4 \text{ m s}^{-2} / 9.8 \text{ m s}^{-2} = 2.8$												
	6b	$t = \frac{2\pi r}{v}$ for whole circle, for $180^\circ$ divide by 2 $t = \frac{2\pi \times 450 \text{ m}}{111 \text{ m s}^{-2}} = 12.7 \text{ s}$												
	7a	Using the same method as 6a, $800 \text{ km h}^{-1} = 222 \text{ m s}^{-1}$												